

SORTING

BY : NISHANT GUPTA

QUICK SORT

- ▣ The running time of the quick sort will lie between $O(n \log n)$ to $O(n^2)$.
- ▣ $O(n \log 2n)$ will be the best case is, means every time the data is divided equally, both sides.
- ▣ It remains in $n \log n$ complexity till there is constant relation like, $1/10$ on left and $9/10$ on right, then $O(n \log 10/9n)$.
- ▣ $O(n^2)$ when the inputted data is either already sorted in ascending or descending way, as in that form a left or right one will have $n-1$ elements at every instant.

SORTING

- ▣ There is algorithm that can sort n random numbers in less than $O(n \log n)$ complexity .
- ▣ $T(n) = \{$ solving trival problem if $n=1;$
- ▣ $\{$
num_pieces * $T(n / \text{subsiquent_sub_prob_size_factor}) + \text{dividing factor} + \text{combining factor}$
- ▣ $\}$ for $n > 1;$
- ▣ Through this the recurrance relation can be made, for any general prob.

MERGE SORT[nlogn/ out place sorting algo]

- ▣ Merge sort(A,p,q)
- ▣ {
- ▣ If($p < q$)
- ▣ $R = p + q / 2$
- ▣ Merge sort(A,p,r)
- ▣ Merge sort(A,r+1,q)
- ▣ merge
- ▣ }

MERGE Function

- ▣ Merging of two sorted sequences if $p_1=n/2$, $p_2=n/2$ than it will take $O(n)$ time complexity,
- ▣ Else if we have two sorted sequences to merge than if let, $p_1=1$, $p_2=m$, than the worst case time is $O(m+1)$ and the best case running time is $O(\min(1,m))$;
- ▣ $T(n)=\{O(1)$ if $n=1$;
- ▣ $\{2*T(n/2) + O(n)$ [for merging] if $n>1$;
- ▣ On solving it comes out to be **$n \log n$** for all the case means worst, average and best.

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RADIX EXCHANGE SORT

- ▣ Sort the array with respect to the leftmost bit.
- ▣ Now partition the array at the point of changing of the bit.
- ▣ RECURSION :

Recursively sort the top subarray, ignoring the leftmost bit.

Recursively sort the bottom subarray, ignoring the leftmost bit.

Time Computation

- ▣ $O(bn)$
- ▣ $T(n) = T(i, b-1) + T(n-1, b-1) + 'n'$ [for the sorting of the leftmost bit! But y is it taking only $O(n)$ time,]
- ▣ Answer is through bucket sort.
- ▣ On solving the above relation we gets $O(bn)$.
- ▣ Radix sort is gud when $b < \log n$,, but else quick sort is better.

STRAIGHT RADIX SORTO(b n)

- ▣ Examines the bits from right to left
- ▣ For($k=0$, to $b-1$)

Sort the array in a stable way, looking only at bit 'k'.

What is the meaning of stable way?

It means that the relative order should be the same as before.

BUCKET SORT $O(n)$

- ▣ This type of sort works when we have numbers of duplicate numbers, and their values are small, like 1,1,2,3,2,1,3,2.
- ▣ Than one bucket is assign to every distinct number. And the rest of the values are added at the end of that bucket again and again in a sort of linked list.
- ▣ Total time is $O(m+n)$, where 'm' is the total numbers of bucket, or the distinct numbers.